

INSTRUCTIONS

- You have 80 minutes to complete the exam.
- This exam has 6 pages and a total of 40 points.
- The exam is closed book, closed notes, closed computer, closed calculator, except one hand-written 8.5" × 11" crib sheet of your own creation and the official Data 100 reference sheet.
- Mark your answers **on the exam itself**. We will *not* grade answers written on scratch paper.
- Please put your name at the top of every page of the exam.

Last name	
First name	
Student ID number	
CalCentral email ( <code>_@berkeley.edu</code> )	
Name of the person to your left	
Name of the person to your right	
<i>All the work on this exam is my own.</i> <b>(please sign)</b>	

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**1. (12 points) Rush Hour**

Fill in both the Python code and the SQL query to produce each result below, assuming that the following tables are stored both as Pandas DataFrames and SQLite tables. **Only the first few rows are shown for each table.** The `trfc` table contains one row per sensor recording of hourly average car speed in mph. The `time` column contains strings that encode the hour of day and whether the time occurred during rush hour. The `dates` table contains one row for all dates in 2019 with their days of the week.

trfc			dates	
time	dt	spd	date	day
hr=01,rush=no	May 1	70	Jan 1	Mon
hr=13,rush=no	May 3	59	May 2	Wed
hr=08,rush=yes	May 29	37	Jun 13	Sat
hr=18,rush=yes	May 3	30	May 4	Thu

(a) (4 pt) Calculate the average speed during rush hour.

Python: `trfc.loc[trfc['time'].str.contains('yes'), 'spd'].mean()`

SQL: `SELECT AVG(spd) FROM trfc WHERE time LIKE '%yes';`

(b) (4 pt) Create a table `t` with one row per recording in `trfc`. Each row should contain the day of week, speed, hour of day as a two-character string, and whether the recording occurred during rush hour (either “yes” or “no”). *Hint:* The correct call to `extract()` takes in a single regex with two captured groups: one for hour of day and one for rush hour. Also, the provided SQL already computes the `hr` column.

Python: `m = trfc.merge(dates, left_on='dt', right_on='date')`

```
m[['hr', 'rush']] = m['time'].str.extract(r'hr=(\d+),rush=(\w+)')
t = m[['day', 'spd', 'hr', 'rush']]
```

SQL: `CREATE TABLE t AS SELECT day, spd, SUBSTR(time, 4, 2) AS hr,
CASE WHEN time LIKE '%no' THEN "no" ELSE "yes" END AS rush
FROM trfc JOIN dates ON dt = date;`

(c) (4 pt) Find the minimum speed in a cluster sample with two clusters: take a SRS of two unique values in `day`, then find the minimum speed across all recordings on those days of the week. Note that there are many speed recordings for every date in May. You may assume that the `t` table is correctly created.

Python: `days = np.random.choice(t['day'].unique(), 2, False)`

```
t.loc[t['day'].isin(days), 'spd'].min()
```

SQL: `SELECT MIN(spd) FROM t WHERE day IN (
SELECT day FROM t GROUP BY day
ORDER BY RANDOM() LIMIT 2
);`

2. (5 points) SAMpling

Suppose that there are ten people in a room and one of these people is named Sam. We will take random samples of these people and compute probabilities associated with these samples. Bubble in the circles corresponding to your answers.

(a) (1 pt) What is the probability that Sam is **not** in a simple random sample of 1 individual?

- $\frac{1}{10}$    
  $\frac{1}{5}$    
  $\frac{2}{5}$    
  $\frac{1}{2}$    
  $\frac{4}{5}$    
  $\frac{9}{10}$    
 None of these

(b) (2 pt) What is the probability that Sam is **not** in a simple random sample of 3 individuals?

- $\frac{1}{10}$    
  $\frac{3}{10}$    
  $\frac{7}{10}$    
  $\frac{9}{10}$    
  $(\frac{3}{10})^3$    
  $(\frac{9}{10})^3$    
 None of these

(c) (2 pt) Suppose we take a sample of 2 individuals by first drawing a simple random sample of size 5, then taking a simple random sample of size 2 from that sample. What is the probability that Sam is **not** in this sample?

- $\frac{1}{10}$    
  $\frac{1}{5}$    
  $\frac{3}{10}$    
  $\frac{1}{2}$    
  $\frac{4}{5}$    
  $(\frac{1}{2} \cdot \frac{9}{10})$    
 None of these

3. (5 points) Go Bears?

$([\text{go}] | [\text{bear}])^+s?!$

Shade in the box for **all** of the strings below that match the regular expression above. Only shade a box if the **whole string** matches the expression, not just a substring. **Do not put a checkmark in the box; shade in the entire box.**

- go!           
 gear?           
 garbs!           
 bearsbears!           
 gobears?!

#### 4. (10 points) Ballers

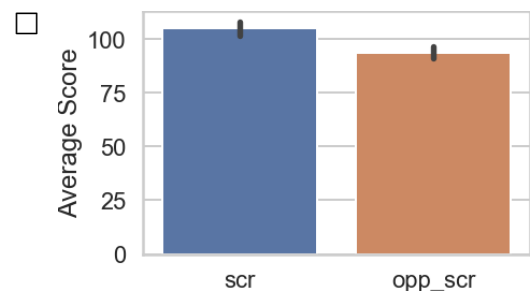
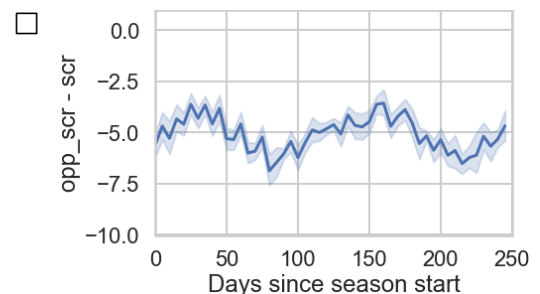
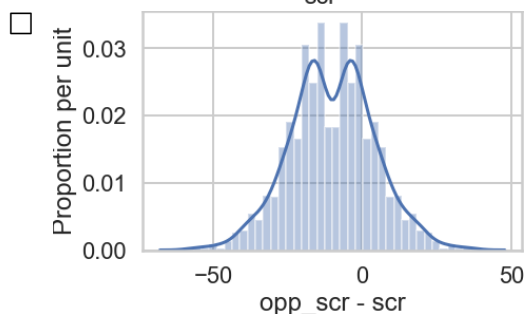
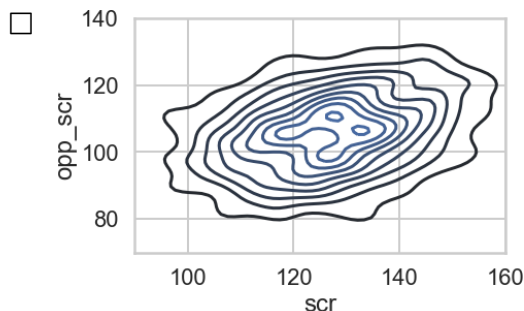
Suppose you have a dataset of 30,000 basketball games played in the NBA over the last 20 years. After conducting EDA, you find that each row in this dataset corresponds to a single game with the six columns described below. You also find that all columns contain duplicate values.

Column	Description	Data Type
date	Date of game	Numeric
team	Home team's name	Nominal
opp	Visiting team's name	Nominal
win	1 if the home team won, else 0	Ordinal
scr	Score of home team	Numeric, between 80 and 170
opp_scr	Score of visiting team	Numeric, between 80 and 170

For each of the following questions, **shade in one or more boxes** corresponding to your answer.

- (a) (2 pt) Given the data types of this dataset, which of the following visualizations are **not** appropriate?
- A histogram of **win**.
  - A histogram of **scr**.
  - A box plot with **team** on the x-axis and **opp\_scr** on the y-axis.
  - A 2D KDE plot with **scr** on the x-axis and **opp\_scr** on the y-axis.
- (b) (2 pt) Which of the following plots will likely suffer from overplotting?
- A scatter plot with dates on the x-axis and number of games played on that date on the y-axis.
  - A scatter plot with **scr** on the x-axis and **opp\_scr** on the y-axis.
  - A scatter plot with **scr** on the x-axis and **win** on the y-axis.
  - A dot plot with **team** on the x-axis and the average of **scr** for each team on the y-axis.
- (c) (2 pt) Which of the following plots show all teams that improved in scoring? (These are the teams with higher scores at later dates.)
- A line plot with one line for every team with **date** on the x-axis and **scr** on the y-axis.
  - A line plot with one line for every team with **date** on the x-axis and **opp\_scr - scr** on the y-axis.
  - One separate line plot for each team with **date** on the x-axis and **scr** on the y-axis.
  - A bar plot with one bar per team and average of the latest five games as bar lengths.
- (d) (2 pt) Which of the following plots show that home teams scored more on average than visiting teams?

Correct answer: all four choices



(e) (2 pt) Suppose you find a linear relationship when you make a scatter plot with `np.log(scr)` on the x-axis and `np.log(opp_scr)` on the y-axis. When you fit a least-squares line on this plot, you find the slope of the line is 2 and the intercept is 5. Which of the following relationships hold?

- `opp_scr = 2 * scr + 5`  
 `log(opp_scr) = log(2 * scr + 5)`  
 `opp_scr = e5 * e2*scr`  
 `opp_scr = e5 * scr2`

### 5. (8 points) Dim Matrices

You perform principal component analysis on a data matrix D using the following Python code from lecture.

```
m = D.shape[0]
X = (D - np.mean(D, axis=0)) / np.sqrt(m)
u, s, vt = np.linalg.svd(X, full_matrices=False)
```

Here are the values of a few expressions executed after running the code above:

Python	Result
<code>s</code>	<code>array([12, 6, 4, 2, 0])</code>
<code>u.shape</code>	<code>(40, 5)</code>
<code>vt[0]</code>	<code>array([0.8, 0, -0.6, 0, 0])</code>

(a) (2 pt) What is the shape of D? Recall that a matrix with 10 rows and 3 columns has shape  $(10 \times 3)$ .

- $(5 \times 5)$ 
  $(5 \times 40)$ 
  $(40 \times 5)$ 
  $(40 \times 40)$

(b) (2 pt) What is the rank of D?

- 0
 1
 2
 3
 4
 5
 6

(c) (2 pt) What percentage of D's total variance is kept if PCA is used to reduce the number of dimensions to 3?

- 12%
 22%
 60%
 92%
 98%
 Not enough information

(d) (2 pt) Suppose the last row in X is: `array([10, 4, -5, 2, 1])`. After projecting this point onto the first principal component, what is the location of this point on the principal component axis?

- 10
 11
 24
 100
 128
 Not enough information