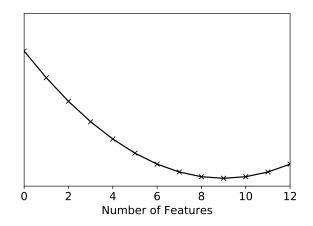
DS 100/200: Principles and Techniques of Data Science Date: March 22, 2019

Discussion #8 Exam Prep

Name:

1. In the process of training linear models with different numbers of features you created the following plot but forgot to include the Y-axis label.



- (a) The Y-axis might represent the training error: \bigcirc A. True \bigcirc B. False
- (b) The Y-axis might represent the bias: \bigcirc A. True \bigcirc B. False
- (c) The Y-axis might represent the test error: \bigcirc A. True \bigcirc B. False
- (d) The Y-axis might represent the variance. \bigcirc A. True \bigcirc B. False
- 2. Consider the following model training script to estimate the training error:

```
1
   X_train, X_test, y_train, y_test =
2
       train_test_split(X, y, test_size=0.1)
3
  model = lm.LinearRegression(fit_intercept=True)
4
  model.fit(X_test, y_test)
5
6
7
   y_fitted = model.predict(X_train)
8
   y_predicted = model.predict(X_test)
9
  training_error = rmse(y_fitted, y_predicted)
10
```

- (a) Line 5 contains a serious mistake. Assuming our eventual goal is to compute the *training error*, which of the following corrects that mistake.
 - A. model.fit(X_train, y_test)
 B. model.fit(X_train, y_train)
 C. model.fit(X, y)
- (b) Line 10 contains a serious mistake. Assuming we already have corrected the mistake in Line 5 which of the following corrects the mistake on Line 10.

A. training_error = rmse(y_train, y_predicted)
B. training_error = rmse(y_train, y_test)
C. training_error = rmse(y_fitted, y_test)
D. training_error = rmse(y_fitted, y_train)

- 3. Which of the following techniques could be used to reduce over-fitting?
 - \bigcirc A. Adding noise to the training data
 - \bigcirc B. Cross-validation to remove features
 - \bigcirc C. Fitting the model on the test split
 - \bigcirc D. Adding features to the training data
- 4. Suppose you are given a dataset $\{(x_i, y_i)\}_{i=1}^n$ where $x_i \in \mathbb{R}$ is a one dimensional feature and $y_i \in \mathbb{R}$ is a real-valued response. To model this data, you choose a model characterized by the following loss function:

$$L(\theta) = \frac{1}{n} \sum_{i=1}^{n} \left(y_i - \theta_0 - x_i^3 \theta_1 \right)^2 + \lambda |\theta_1|$$
(1)

For the following statements, indicate whether it is True or False.

(a) This model includes a bias/intercept term.

 \bigcirc A. True \bigcirc B. False

(b) As λ decreases to smaller values, the model will reduce to a constant θ_0

 \bigcirc A. True \bigcirc B. False

(c) Larger λ values help reduce the chances of overfitting.

 \bigcirc A. True \bigcirc B. False

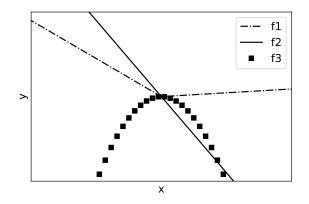
(d) Increasing λ decreases model variance.

 \bigcirc A. True \bigcirc B. False

(e) The training error should be used to determine the best value for λ .

 \bigcirc A. True \bigcirc B. False

5. Use the following plot to answer each of the following questions about convexity:

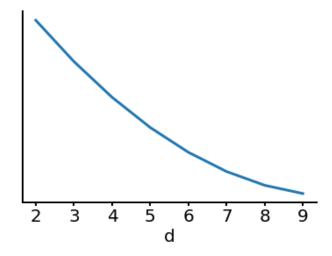


- (a) $f_1(x) = \max(0.01x, -x)$ is convex. \bigcirc A. True \bigcirc B. False (b) $f_2(x) = -2x$ is convex. \bigcirc A. True \bigcirc B. False (c) $f_3(x) = -x^2$ is convex. \bigcirc A. True \bigcirc B. False (d) $f_4(x) = f_1(x) + f_2(x)$ is convex. \bigcirc A. True \bigcirc B. False
- 6. In class, we showed that the expected squared error can be decomposed into several important terms:

$$\mathbb{E}[(Y - f_{\hat{\theta}}(x))^2] = \sigma^2 + (h(x) - \mathbb{E}[f_{\hat{\theta}}(x)])^2 + \mathbb{E}[(\mathbb{E}[f_{\hat{\theta}}(x)] - f_{\hat{\theta}}(x))^2].$$

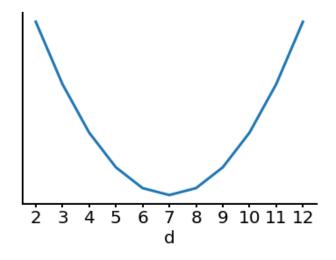
- (a) For which of the following reasons are we taking an expectation? In other words, what are the sources of randomness that we are considering in the derivation of the bias-variance tradeoff?
 - \Box A. We chose arbitrary features when doing feature engineering.
 - \Box B. We drew random samples from some larger population when we built our training set.

- □ C. There is some noise in the underlying process that generates our observations Y from our features.
- □ D. Our x values could have had missing or erroneous data, e.g. participants misreading a question on a survey.
- \Box E. None of the Above.
- (b) Which of the following do we treat as fixed? Select all that apply.
 - \Box A. $\hat{\theta}$
 - \Box B. σ^2
 - \Box C. h(x)
- (c) By decreasing model complexity, we are able to decrease σ^2 .
 - \bigcirc A. True
 - \bigcirc B. False
- 7. Your team would like to train a machine learning model in order to predict the next YouTube video that a user will click on based on m features for each of the previous d videos watched by that user. In other words, the total number of features is $m \times d$. You're not sure how many videos to consider.
 - (a) Your colleague generates the following plot, where the value d is on the x axis. However, they forgot to label the y-axis.



Which of the following could the y axis represent? Select all that apply.

- \Box A. Training Error
- \square B. Validation Error
- \Box C. Bias
- \Box D. Variance
- (b) Your colleague generates the following plot, where the value d is on the x axis. However, they forgot to label the y-axis.



Which of the following could the y axis represent? Select all that apply.

- \Box A. Training Error
- \Box B. Validation Error
- \square C. Bias
- \Box D. Variance
- 8. Elastic Net is a regression technique that combines L_1 and L_2 regularization. It is preferred in many situations as it possesses the benefits of both LASSO and Ridge Regression. Minimizing the L2 loss using Elastic Net is as follows, where $\lambda_1, \lambda_2 \ge 0$, $\lambda_1 + \lambda_2 = \lambda, \lambda \ge 0$.

$$\hat{\theta} = \arg\min_{\theta} \frac{1}{n} \sum_{i} (y_i - \theta x)^2 + \lambda_1 \sum_{j=1}^p |\theta_j| + \lambda_2 \sum_{j=1}^p \theta_j^2$$

Suppose our goal was to get sparse parameters, i.e. we want as many parameters as possible to be zero. Which of the following choices for λ_1, λ_2 are most consistent with this goal, assuming $\lambda = 1$? There is only one correct answer.

- $\bigcirc A. \ \lambda_1 = 0, \lambda_2 = 1$ $\bigcirc B. \ \lambda_1 = 0.5, \lambda_2 = 0.5$ $\bigcirc C. \ \lambda_1 = 1, \lambda_2 = 0$
- 9. What happens to bias and variance as we increase the value of λ ? Assume $\lambda_2 = \lambda_1$. There is only one correct answer in each part. You will be asked to justify why in the next question.
 - (a) Bias:
 - \bigcirc A. Bias goes up
 - \bigcirc B. Bias stays the same
 - \bigcirc C. Bias goes down

- (b) Variance:
 - \bigcirc A. Variance goes up
 - \bigcirc B. Variance stays the same
 - \bigcirc C. Variance goes down
- 10. Justify why by marking the true statements. Select all that apply for each part.
 - (a) Bias:
 - \Box A. Bias goes down because increasing λ reduces over fitting.
 - \square B. Bias goes down because bias is minimized when $\lambda_2 = \lambda_1$.
 - \Box C. Bias goes up because increasing λ penalizes complex models, limiting the set of possible solutions.
 - \Box D. Bias goes up because the loss function becomes non-convex for sufficiently large λ .
 - \Box E. None of the above
 - (b) Variance:
 - \Box A. Variance goes down because increasing λ encourages the value of the loss to decrease.
 - \square B. Variance goes down because increasing λ penalizes large model weights.
 - \Box C. Variance goes up because because increasing λ increases bias.
 - \Box D. Variance goes up because increasing λ increases the magnitude of terms in the loss function.
 - \Box E. None of the above
- 11. What happens to the model parameters $\hat{\theta}$ as $\lambda \to \infty$, i.e. what is $\lim_{\lambda \to \infty} \hat{\theta}$? Select all that apply.
 - \Box A. Converge to 0.
 - \square B. Diverge to infinity.
 - \square C. Converge to values that minimize the L2 loss.
 - \Box D. Converge to equal but non-zero values.
 - \Box E. Converge to a sparse vector.